



# Relationships of acoustic quantities associated with a plane progressive acoustic sound wave

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|   | $\xi$                                  | $v$                   | $a$                                    | $\rho$                        | $J$                                   | $E$                                      | $P_{ac}$   |
|---|--|-----------------------|--|-------------------------------|---------------------------------------|--|--|
| Particle displacement $\xi$                       | -                                      | $\frac{v}{\omega}$    | $\frac{a}{\omega^2}$                   | $\frac{\rho}{\omega \cdot Z}$ | $\frac{1}{\omega} \sqrt{\frac{J}{Z}}$ | $\frac{1}{\omega} \sqrt{\frac{E}{\rho}}$ | $\frac{1}{\omega} \sqrt{\frac{P_{ac}}{Z \cdot A}}$ |
| Particle velocity $v$                             | $\xi \cdot \omega$                     | -                     | $\frac{a}{\omega}$                     | $\frac{\rho}{Z}$              | $\sqrt{\frac{J}{Z}}$                  | $\sqrt{\frac{E}{\rho}}$                  | $\sqrt{\frac{P_{ac}}{Z \cdot A}}$                  |
| Particle acceleration $a$                         | $\xi \cdot \omega^2$                   | $v \cdot \omega$      | -                                      | $\frac{\rho \cdot \omega}{Z}$ | $\omega \sqrt{\frac{J}{Z}}$           | $\omega \sqrt{\frac{E}{\rho}}$           | $\omega \sqrt{\frac{P_{ac}}{Z \cdot A}}$           |
| Sound pressure $p$                                | $\xi \cdot \omega \cdot Z$             | $v \cdot Z$           | $\frac{a \cdot Z}{\omega}$             | -                             | $\sqrt{J \cdot Z}$                    | $c \sqrt{\rho \cdot E}$                  | $\sqrt{\frac{P_{ac} \cdot Z}{A}}$                  |
| Sound intensity $J$<br>$= P_{ak} / A = p \cdot v$ | $\xi^2 \cdot \omega^2 \cdot Z$         | $v^2 \cdot Z$         | $\frac{a^2 \cdot Z}{\omega^2}$         | $\frac{\rho^2}{Z}$            | -                                     | $E \cdot c$                              | $\frac{P_{ac}}{A}$                                 |
| Sound energy density $E$ or $w$                   | $\xi^2 \cdot \omega^2 \cdot \rho$      | $v^2 \cdot \rho$      | $\frac{a^2 \cdot \rho}{\omega^2}$      | $\frac{\rho^2}{Z \cdot c}$    | $\frac{J}{c}$                         | -  | $\frac{P_{ac}}{c \cdot A}$                         |
| Sound power $P_{ac}$<br>$= J \cdot A$             | $\xi^2 \cdot \omega^2 \cdot Z \cdot A$ | $v^2 \cdot Z \cdot A$ | $\frac{a^2 \cdot Z \cdot A}{\omega^2}$ | $\frac{\rho^2 \cdot A}{Z}$    | $J \cdot A$                           | $E \cdot c \cdot A$                      | -  |

White = linear sound field strength and gray = squared sound energy strength.

Specific acoustic impedance  $Z = \rho \cdot c = \frac{p}{v} = \frac{J}{v^2} = \frac{p^2}{J}$  in  $\frac{N \cdot s}{m^3}$

Density of air  $\rho$  in  $\frac{kg}{m^3}$  is 1.204 kg/m<sup>3</sup> at 20 °C

Angular frequency  $\omega = 2 \cdot \pi \cdot f$

Frequency  $f$  in Hz =  $\frac{1}{s}$  in air of 20 °C:  $Z = 413 \frac{N \cdot s}{m^3}$

Area through a unit area normal to the direction  $A$  in m<sup>2</sup>

Displacement of air particles (excursion amplitude)  $\xi$  in m

Particle velocity (velocity amplitude)  $v$  in  $\frac{m}{s}$

Particle acceleration  $a$  in  $\frac{m}{s^2}$

Sound pressure (excess pressure)  $p = \frac{F}{A}$  in  $\frac{N}{m^2} = Pa$

Sound intensity  $J = p \cdot v = \frac{P_{ak}}{A}$  in  $\frac{W}{m^2}$

Sound energy density  $E$  or  $w = \frac{J}{c}$  in  $\frac{W \cdot s}{m^3}$

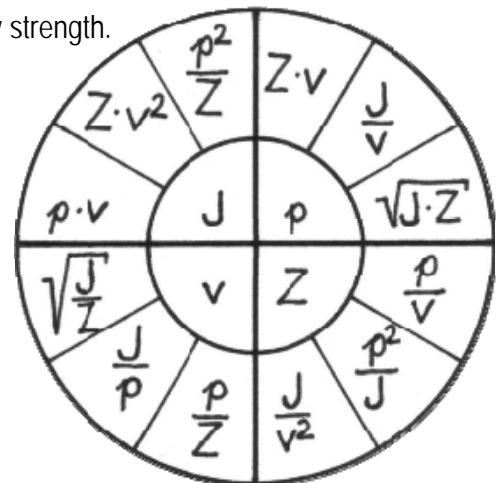
Here is 1 Joule  $J = W \cdot s = N \cdot m$

Sound power  $P_{ac} = J \cdot A$  in W

Speed of sound  $c$  in m/s (at 20 °C is  $c = 343$  m/s)

Because  $1 W \cdot s = 1 N \cdot m$ , the sound energy density is  $1 W \cdot s / m^3 \equiv 1 N \cdot m / m^3 = 1 N / m^2$  and that is the unit of a sound pressure in pascals!

To remember:  $W \cdot s = N \cdot m = J$  (joule).



To the comparison: U means here V

